Problem 3

In the following problems, find the limit of the given sequence as $n \to \infty$.

$$\frac{(-1)^n \sqrt{n+1}}{n}$$

Solution

Take the limit as $n \to \infty$.

$$\lim_{n \to \infty} \frac{(-1)^n \sqrt{n+1}}{n} = \lim_{n \to \infty} (-1)^n \sqrt{\frac{1}{n^2}(n+1)}$$
$$= \lim_{n \to \infty} (-1)^n \sqrt{\frac{1}{n} + \frac{1}{n^2}}$$
$$= \left[\lim_{n \to \infty} (-1)^n\right] \left(\lim_{n \to \infty} \sqrt{\frac{1}{n} + \frac{1}{n^2}}\right)$$
$$= \left[\lim_{n \to \infty} (-1)^n\right] (0)$$
$$= 0$$